

$$5 \quad -\frac{1}{2} + 2a - 3b + \frac{1}{2} - a + 3b \quad [a]$$

$$7 \quad -\frac{2}{3}a + a^2 - \left(-\frac{1}{3}a\right) - \frac{1}{2}a^2$$

$$8 \quad 0,5x - 0,2xy + \frac{1}{2}xy - x$$

$$9 \quad 2x^{-4} - 3x^{-2} + x^{-4} - x^{-2} \quad [3x^{-4} - 4x^{-2}]$$

$$11 \quad \frac{4}{3}x^4 - \frac{1}{2}x^3 + \frac{1}{4}x^4 + 0,5x^3$$

$$6 \quad 7a^5 - (-2a) - (+8a) + (-a^5) [6a^5 - 6a]$$

$$\left[\frac{1}{2}a^2 - \frac{1}{3}a\right]$$

$$[-0,5x + 0,3xy]$$

$$10 \quad -(-xy) + 4xy - \frac{5}{2} + (-5xy) + \frac{3}{2} \quad [-1]$$

$$\left[\frac{19}{12}x^4\right]$$

$$20 \quad -x^2 \cdot \left(+\frac{2}{3}xy^4\right) \cdot \left(-\frac{3}{8}y^3\right) \quad \left[\frac{1}{4}x^3y^9\right]$$

$$21 \quad +\frac{2}{3}xyz^3 \cdot \left(-\frac{3}{10}x^2\right) \cdot (-2x^4y^2z^5) \quad \left[\frac{2}{5}x^7y^3z^8\right]$$

$$22 \quad \frac{2}{5}xy \cdot (-0,2x^2y^3) \cdot \left(+\frac{25}{4}y^4\right) \cdot 2x \quad [-x^4y^8]$$

$$42 \left[-2a \cdot (-3ab) + a^2b - b \cdot \left(-\frac{1}{2}a^2 \right) \right] \cdot \left(a + \frac{3}{2}a \right) \left[\frac{75}{4}a^3b \right]$$

Calcolare le seguenti potenze:

- 69 $(-5a^2b^3)^2$; $\left(+\frac{1}{2}ab^2c\right)^2$ $\left[25a^4b^6; \frac{1}{4}a^2b^4c^2\right]$
- 70 $\left(-\frac{2}{3}xy^5\right)^3$; $\left(+\frac{1}{4}x^3y^2z\right)^3$ $\left[-\frac{8}{27}x^3y^{15}; \frac{1}{64}x^9y^6z^3\right]$
- 71 $(-2a^5bc^3)^4$; $(+3ab^6)^0$ $[16a^{20}b^4c^{12}; 1]$
- 72 $(-a^2b^3)^2$; $\left(-\frac{1}{2}ab^3\right)^3$ $\left[a^4b^6; -\frac{1}{8}a^3b^9\right]$

$$78 \quad \left(-\frac{3}{2}ab - 0,5ab\right)^3 \cdot \left(1 - \frac{2}{3}\right)^2 \quad \left[-\frac{8}{9}a^3b^3\right]$$

$$79 \quad \left(\frac{1}{2}ab - 3ab\right) : \left(a^2 - 3a^2 + \frac{1}{2}a^2\right)^0 \quad \left[-\frac{5}{2}ab\right]$$

$$80 \quad (-0,2x^4 + 0,6x^4)^2 : \left(3x - \frac{5}{2}x\right) \quad [0,32x^7]$$

$$81 \quad \left[(-2a)^2 \cdot \left(\frac{1}{2}ab\right)^3 - a^5b^3\right] : (a^2b) \quad \left[-\frac{1}{2}a^3b^2\right]$$

Trovare il M.C.D. ed il m.c.m. dei seguenti gruppi di monomi interi:

$$106 \quad 3a^3b^2; \quad 6a^4b^3; \quad 27a^2b^5 \qquad [3a^2b^2; 54a^4b^5]$$

$$107 \quad a^4b^2c^6; \quad 3ab^5; \quad 2a^6bc^4 \qquad [ab; 6a^6b^5c^6]$$

$$108 \quad 10x^2y^3; \quad 15x^7y; \quad 45x^3y^4z^5 \qquad [5x^2y; 90x^7y^4z^5]$$

$$109 \quad 4x^3y^2; \quad 3x^2z^3; \quad 5yz \qquad [1; 60x^3y^2z^3]$$

$$114 \quad \left(\frac{1}{2} - x^3 + 3x - y \right) + \left(\frac{3}{2} + x^3 - 2x - 8y \right) \quad [2 + x - 9y]$$

$$115 \quad \left(\frac{1}{3} ab - \frac{1}{2} a^2 + 1 \right) + \left(-\frac{2}{3} ab - \frac{3}{2} a^2 + \frac{1}{3} \right) \quad \left[-\frac{1}{3} ab - 2a^2 + \frac{4}{3} \right]$$

$$116 \quad \left(x^4 - \frac{x^2 y}{3} + 4x - 2y \right) + (2y - 6x) + \left(\frac{2x^2 y}{3} - x^4 \right) \quad \left[\frac{1}{3} x^2 y - 2x \right]$$

$$117 \quad (8x^2 - 3xy + 4) + (-2xy - 5x^2 - 4 + y^2) \quad [3x^2 - 5xy + y^2]$$

Eseguire le seguenti moltiplicazioni tra un monomio ed un polinomio:

145 $2a^2 \cdot (ab - a^3 + 1)$;

$$[2a^3b - 2a^5 + 2a^2]$$

146 $xy^2 \cdot (-x + 2xy + y^2)$

$$[-x^2y^2 + 2x^2y^3 + xy^4]$$

147 $\frac{1}{2} a^3b \cdot (-2 + 4ab)$

$$[-a^3b + 2a^4b^2]$$

$$\cdot 148 \quad \frac{x^2y}{3} \cdot \left(x^4 - 9xy^2 + \frac{3}{2}y \right)$$

$$\left[\frac{x^6y}{3} - 3x^3y^3 + \frac{x^2y^2}{2} \right]$$

$$\cdot 149 \quad -2x^4 \cdot \left(\frac{2x}{3} - \frac{4}{5}xy^3 - \frac{1}{2} \right)$$

$$\left[-\frac{4}{3}x^5 + \frac{8}{5}x^5y^3 + x^4 \right]$$

$$\cdot 150 \quad -\frac{a^5b^2}{2} \cdot \left(-a^5 + 4ab^2 - \frac{ab^3}{2} \right)$$

$$\left[\frac{1}{2}a^{10}b^2 - 2a^6b^4 + \frac{1}{6}a^6b^5 \right]$$

Eseguire le seguenti moltiplicazioni tra polinomi:

169 $(3a - 2b) \cdot (a + 2b)$

$[3a^2 - 4b^2 + 4ab]$

170 $(a^2 - 3b + 1)(-2 + a^2 - b)$

$[-a^2 + a^4 - 4a^2b + 5b + 3b^2 - 2]$

171 $(3 - x + 2y)(x - 3y + 1)$

$[-x^2 - 6y^2 + 5xy + 2x - 7y + 3]$

172 $\left(-\frac{y}{2} + 2x - \frac{3}{2}\right)(-x + 2y + 1)$

$\left[-2x^2 - y^2 + \frac{9}{2}xy + \frac{7}{2}x - \frac{7}{2}y - \frac{3}{2}\right]$

Eseguire i seguenti prodotti notevoli:

Quadrati di binomi

195 $(2a + 3b)^2$

$$[4a^2 + 12ab + 9b^2]$$

196 $\left(\frac{1}{2}a - 2b\right)^2$

$$\left[\frac{a^2}{4} - 2ab + 4b^2\right]$$

197 $\left(-\frac{3}{2}a + 2a^2\right)^2$

$$\left[\frac{9}{4}a^2 - 6a^3 + 4a^4\right]$$

198 $(x^2 + 2xy)^2;$

$$\left(\frac{1}{4}x - 2y\right)^2$$

199 $\left(\frac{a^2}{4} - 4\right)^2$

$$\left[\frac{a^4}{16} - 2a^2 + 16\right]$$

200 $\left(xy - \frac{1}{2}x^2y^3\right)^2$

$$\left[x^2y^2 - x^3y^4 + \frac{1}{4}x^4y^6\right]$$

Cubi di binomi

$$203 \quad (2a + b)^3 \qquad [8a^3 + 12a^2b + 6ab^2 + b^3]$$

$$204 \quad (a + 3b)^3; \qquad (2a + 3b)^3$$

$$205 \quad \left(\frac{a}{3} + 2b\right)^3 \qquad \left[\frac{a^3}{27} + \frac{2a^2b}{3} + 4ab^2 + 8b^3\right]$$

$$206 \quad \left(\frac{1}{3}a^2 - ab\right)^3 \qquad \left[\frac{1}{27}a^6 - \frac{1}{3}a^5b + a^4b^2 - a^3b^3\right]$$

$$207 \quad (ab - 3b^2)^3; \qquad (2a - 5b)^3$$

$$208 \quad \left(\frac{2}{3}x^2 - \frac{1}{3}y^3\right)^3 \qquad \left[\frac{8}{27}x^6 - \frac{4}{9}x^4y^3 + \frac{2}{9}x^2y^6 - \frac{1}{27}y^9\right]$$

$$209 \quad \left(-3x - \frac{1}{9}xy\right)^3 \qquad \left[-27x^3 - 3x^3y - \frac{1}{9}x^3y^2 - \frac{1}{729}x^3y^3\right]$$

$$210 \quad \left(-2a^2 - \frac{1}{2}ab^3\right)^3; \qquad (a + 3a^2b)^3$$

$$211 \quad \left(\frac{a}{b} - b\right)^3 \qquad \left[\frac{a^3}{b^3} - 3\frac{a^2}{b} + 3ab - b^3\right]$$

$$\bullet 184 \quad \frac{3}{2}a(2a+1-b) - (-a+b+4)(a-b) - 4a(a-1) - \frac{3}{2}a \quad \left[-\frac{7}{2}ab + b^2 + \dots \right]$$

$$\bullet 185 \quad (a-2b)(a+2b) - a(a+2b) - b(-4b-2a)$$

$$186 \quad 2a(a-3b)(a+b) - b(2a+b)(a-b) \quad [2a^3 + b^3 - 5ab^2 - 6a^2b]$$

$$\times 187 \quad \frac{2}{3}x^2(x+y-1) - 2x(x+1)(x-y) - \frac{4}{3}x^2(2y-x) \quad \left[-\frac{8}{3}x^2 + 2xy \right]$$

$$201 \quad (-2x - 3y^2)^2$$

$$[4x^2 + 12xy^2 + 9y^4]$$

$$202 \quad \left(\frac{4}{5}x^2 - \frac{5}{2}xy^2\right)^2$$

$$\left[\frac{16}{25}x^4 - 4x^3y^2 + \frac{25}{4}x^2y^4\right]$$

Somma per differenza

$$225 \quad (a + 2b)(a - 2b)$$

$$[a^2 - 4b^2]$$

$$226 \quad \left(\frac{1}{2}a^2 + 2b\right)\left(\frac{1}{2}a^2 - 2b\right);$$

$$(3a - b^2)(3a + b^2)$$

$$227 \quad (3x^2y - y)(3x^2y + y)$$

$$[9x^4y^2 - y^2]$$

$$228 \quad \left(\frac{1}{2}xy + \frac{1}{3}\right)\left(\frac{1}{2}xy - \frac{1}{3}\right);$$

$$(x^2y + y^3)(x^2y - y^3)$$

Eseguire le operazioni indicate:

• 245 $(2x - 1)^2 + \left(\frac{3}{2}x - 1\right)^2$

$\left[\frac{25}{4}x^2 - 7x + 2\right]^*$

• 246 $(x + 2y)^2 - (x - 2y)^2 - 8xy$

[0]

$$307 \quad (x^5 - x^2 + 2x^3) : (-x^2)$$

$$[-x^3 + 1 - 2x]$$

$$308 \quad \left(\frac{2}{3}a^4 - \frac{1}{3}a^2 + a\right) : \left(\frac{1}{2}a\right)$$

$$[2a^3 - a + 3]$$

$$309 \quad \left(-a^6b^2 + 2a^5b^3 - \frac{ab^4}{2}\right) : (-ab^2)$$

$$\left[a^5 - 2a^4b + \frac{1}{2}b^2\right]$$

$$310 \quad \left(\frac{3}{2}a^5 - \frac{4}{3}a^2 + \frac{1}{3}a^3\right) : \left(\frac{2}{3}a^2\right)$$

$$\left[\frac{9}{4}a^3 - 2 + \frac{1}{2}a\right]$$

$$340 \quad \left(-x^2 + \frac{3}{2}x^3 - 2\right) : (3x^2 + 2x)$$

$$\left[Q = \frac{1}{2}x - \frac{2}{3}; R = \frac{4}{3}x - 2\right]$$

$$341 \quad \left(-\frac{3}{5}a^4 - 2 - 6a^3 - \frac{1}{5}a\right) : (-3a^3 - 1)$$

$$\left[Q = \frac{1}{5}a + 2; R = 0\right]$$

$$342 \quad \left(\frac{8}{3}x^7 + \frac{2}{3}x^2 - 1\right) : (1 - 4x^5)$$

$$\left[Q = -\frac{2}{3}x^2; R = \frac{4}{3}x^2 - 1\right]$$

Eseguire le seguenti divisioni con la regola di Ruffini ed effettuare poi la verifica nei casi in cui non è riportato il risultato:

✕ 362 $(2a^3 - a^2 + 3a - 1) : (a - 1)$ $[Q = 2a^2 + a + 4; R = 3]$

✕ 363 $(-a^2 + 1 - 3a) : (a + 1)$ $[Q = -a - 2; R = 3]$

• 364 $(3a^4 - a^2 + 2 - a) : (a - 2)$ $[Q = 3a^3 + 6a^2 + 11a + 21; R = 44]$

✕ 365 $(x - 2x^2 - 3x^4) : (x + 2)$ $[Q = -3x^3 + 6x^2 - 14x + 29; R = -58]$

✕ 366 $(x^2 - x^3 + 18) : (x - 3)$ $[Q = -x^2 - 2x - 6; R = 0]$

Eseguire le seguenti divisioni con la regola di Ruffini ed effettuare poi la verifica nei casi in cui non è riportato il risultato:

• 383 $(2x^2 - 3x + 1) : (2x + 1)$

$$[Q = x - 2; R = 3]$$

• 384 $(3x^2 - 3 + 2x) : (3x - 2)$

$$\left[Q = x + \frac{4}{3}; R = -\frac{1}{3} \right]$$

• 385 $(a^2 - 2a + 4) : (3a + 1)$

• 386 $(8a^3 - 27) : (2a - 3)$

$$[Q = 4a^2 + 6a + 9; R = 0]$$

Scomporre i seguenti polinomi raccogliendo i fattori comuni:

$$1 \quad 2a^2b + 6ab^2; \quad 3ab + 6a^2 + 9a \quad [2ab(a + 3b); \dots]$$

$$2 \quad 8x^4 - 4x^3 + 2x^2; \quad 25x^3y^4 - 5x^2y^3 + 5x^2y^2 \quad [2x^2(4x^2 - 2x + 1); \dots]$$

$$3 \quad 2a^3x^2y - 4a^2x^3y^2 + 6ax^2y^2; \quad 0,20a^2x^3 - 0,15a^3x + 0,40ax^2$$

$$4 \quad \frac{1}{3}ab^3c^2 - \frac{1}{9}a^2bc^4;$$

$$5 \quad 15x^2y^3 - 6x^3y^2 - 3xy^2;$$

$$6 \quad 25ab^2c - 30ac^2 + 10a^2b;$$

$$7 \quad 6a^4 + 9a^3 - 12a^2;$$

$$3x^2 - 27x^3y + 3x^2y^2$$

$$12a^2b^3 + 30a^3b + 6ab$$

$$x^5y^3 - x^2y + x^4y^5 + 2x^3y^2$$

$$0,5b^3 - 0,25b^5 + \frac{1}{2}b^2$$

Scomporre i seguenti polinomi ricordando che $a^2 - b^2 = (a + b)(a - b)$:

46 $a^2 - b^2$;

$4a^2 - 25$;

$a^2 - 9b^2$

47 $4x^2 - 9y^2$;

$\frac{25}{9} - a^2$;

$x^2 - \frac{9}{4}$

48 $64x^2 - 1$;

$x^6 - y^4$;

$1 - 4y^2x^2$

49 $x^4 - y^4$;

$64 - a^4$;

$16 - a^4$

50 $81x^4 - 16y^4$;

$100 - 81a^2$;

$a^8 - 1$

Scomporre i seguenti polinomi tenendo presente il prodotto notevole quadrato di un polinomio:

• 69 $a^2 + b^2 + 2ab;$ $a^2 + 4b^2 - 4ab$ • 70 $4x^2 + 9y^2 + 12xy;$ $x^2 + 1 - 2x$

71 $\frac{x^2}{4} + 4 + 2x;$ $\frac{9}{4}x^2 + 25y^2 + 15xy$ 72 $4a^2b^2 + \frac{1}{16} - ab;$ $a^2 + 16 - 8a$

• 73 $8x^2 + 18y^2 - 24xy;$ $2ax^2 + 2a - 4ax$

74 $a^3 + 4ab^2 + 4a^2b;$ $a^2 + b^2 + c^2 + 2ab + 2ac + 2bc$

Scomporre i seguenti polinomi tenendo presenti gli esercizi precedenti:

- 85 $a^2 + 2ab + b^2 - 1$; $x^2 + y^2 - 2xy - 4$ 86 $4x^2 + y^2 + 4xy - z^2$; $a^2 - 4ab + 4b^2 - 9$
- 87 $25 - 10x + x^2 - y^2$; $9a^2 + 12ab + 4b^2 - 1$ 88 $9 - a^2 - b^2 + 2ab$; $1 - x^2 - \frac{1}{4}y^2 + xy$
- 89 $4a^2b^2 - 9a^2 - b^2 + 6ab$; $x^2 + y^2 - 2xy - a^2 - b^2 - 2ab$

Scomporre i seguenti polinomi tenendo presente che $a^3 \pm b^3 = (a \pm b)(a^2 \mp ab + b^2)$:

112 $a^3 - 8$;

114 $8x^3 - 27$;

116 $a^6 - b^3$;

$8a^3 + 27$

$a^3b^3 + \frac{1}{27}$

$9x^3 - 243$

113 $a^3 - 1$;

115 $\frac{1}{8} - 64x^3y^6$;

117 $\frac{3}{8} + 81a^3$;

$b^3 + 8$

$a^6 + b^3$

$2a^3 - 54$

Scomporre i seguenti trinomi:

Memoranda la regola di Ruffini

• 136 $x^2 - 3x + 2;$

$x^2 - 2x - 3$

• 137 $x^2 + 8x + 7;$

$x^2 + x - 12$

• 138 $x^2 + 10x - 11;$

$x^2 + 9x + 20$

• 139 $x^2 - 4x - 12;$

$a^2 - 15a + 56$

• 140 $b^2 + 7b + 10;$

$b^2 + b - 72$

• 141 $2x^2 - 2x - 40;$

$3x^2 + 21x + 36$

• 142 $3a^3 + 12a^2 - 63a;$

$x^4 - 12x^3 + 35x^2$

• 143 $5b^3 - 10b^2 - 15b;$

$-x^3 - 2x^2 + 8x$

Ridurre ai minimi termini le seguenti frazioni algebriche letterali:

$$1 \quad \frac{4xy}{6x^2} ; \quad \frac{3x^3y^2}{12xy^4} ; \quad \frac{15a^6b^2c}{18a^2bc}$$

$$\left[\frac{2y}{3x} ; \frac{x^2}{4y^2} ; \frac{5a^4b}{6} \right]$$

$$2 \quad \frac{5ab}{10a^2} ; \quad \frac{7a^6b^3}{21a^2b^3} ; \quad \frac{18a^9}{6a^3b^2}$$

$$\left[\frac{b}{2a} ; \frac{a^4}{3} ; \frac{3a^6}{b^2} \right]$$

$$3 \quad -\frac{6ab^2c}{9a^2c^2} ; \quad -\frac{10x^4y^3}{15xy^2z} ; \quad \frac{7a}{21a^2b}$$

$$\left[-\frac{2b^2}{3ac} ; -\frac{2x^3y}{3z} ; \frac{1}{3ab} \right]$$

$$16 \quad \frac{7a^2 - 7b^2}{3a + 3b} ; \quad \frac{4a^2 - 1}{4a^2 + 1 + 4a} \quad \left[\frac{7(a - b)}{3} ; \frac{2a - 1}{2a + 1} \right]$$

$$17 \quad \frac{4x^2y^2 + 1 + 4xy}{4x^2y^2 - 1} ; \quad \frac{x^3 + y^3 + 3x^2y + 3xy^2}{4x^2 + 8xy + 4y^2} \quad \left[\frac{2xy + 1}{2xy - 1} ; \frac{x + y}{4} \right]$$

$$18 \quad \frac{a^3 - 3a^2 + 3a - 1}{a^2 - 1} ; \quad \frac{a^2 + 2a + 1}{a^3 + 1 + 3a + 3a^2} \quad \left[\frac{(a - 1)^2}{a + 1} ; \frac{1}{a + 1} \right]$$

$$19 \quad \frac{x^3 - 1}{x^2 - 2x + 1} ; \quad \frac{x^3 + 1}{3x + 3} \quad \left[\frac{x^2 + x + 1}{x - 1} ; \frac{x^2 - x + 1}{3} \right]$$

$$20 \quad \frac{a^3b^3 - 8}{2ab - 4} ; \quad \frac{1 - 27a^3}{1 + 27a^3 + 9a^2 + 27a^2} \quad \left[\frac{a^2b^2 + 2ab + 4}{2} ; \frac{1 + 3a + 9a^2}{3} \right]$$

$$21 \quad \frac{14x - 7y}{4x^2 - y^2} ; \quad \frac{a^2 - 5a + 6}{a^2 - 4a + 4} \quad \left[\frac{7}{2x + y} ; \frac{a - 3}{a - 2} \right]$$

$$22 \quad \frac{x^2 + 5x + 6}{x^2 + 4x + 4} ; \quad \frac{2x^2 - 10x + 12}{x^2 - 6x + 9} \quad \left[\frac{x + 3}{x + 2} ; \frac{2(x - 2)}{x - 3} \right]$$

$$23 \quad \frac{x^4 - 16}{x^4 + 16 - 8x^2} ; \quad \frac{16 - a^4}{4 + a^2 - 4a} \quad \left[\frac{x^2 + 4}{x^2 - 4} ; \frac{(4 + a^2)(2 + a)}{2 - a} \right]$$

$$24 \quad \frac{8x^3 - y^3}{4x^2 - y^2}; \quad \frac{8x^3 + y^3}{2xy + y^2}$$

$$\left[\frac{4x^2 + 2xy + y^2}{2x + y}; \frac{4x^2 - 2xy + y^2}{y} \right]$$

$$25 \quad \frac{4a^2 + 12ab + 9b^2}{14a + 21b}; \quad \frac{4a^2 + 20ab + 25b^2}{18a + 45b}$$

$$\left[\frac{2a + 3b}{7}; \dots \right]$$

$$26 \quad \frac{27x^3 - y^3}{18x^2 + 6xy + 2y^2}; \quad \frac{8a^3 - b^3}{12a^2 + 6ab + 3b^2}$$

$$\left[\frac{3x - y}{2}; \dots \right]$$

$$27 \quad \frac{a^2 + 2a + 1}{a^3 - a}; \quad \frac{4b^2 + 4b + 1}{8b^3 - 2b}; \quad \frac{a^3 + 1}{4a^3 - 4a^2 + 4a}$$

$$\left[\frac{a + 1}{a(a - 1)}; \dots \right]$$

$$28 \quad \frac{a^2 - 3a - 4}{a^2 - 4a - 5}; \quad \frac{a^2 - 3a + 2}{a^2 - 4a + 3}; \quad \frac{x^4 - 2x^2 + 1}{x^3 - x + 3x^2 - 3}$$

$$\left[\frac{a - 4}{a - 5}; \dots \right]$$

Ridurre le seguenti frazioni letterali al minimo comune denominatore:

$$47 \quad \frac{2}{3x}; \quad \frac{1}{6x^2}; \quad -\frac{y}{2x} \qquad \left[\frac{4x}{6x^2}; \quad \frac{1}{6x^2}; \quad \frac{3xy}{6x^2} \right]$$

$$48 \quad \frac{a}{3b^2}; \quad \frac{3}{2ab}; \quad \frac{5b}{15a^2} \qquad \left[\frac{2a^3}{6a^2b^2}; \quad \frac{9ab}{6a^2b^2}; \quad \frac{2b^3}{6a^2b^2} \right]$$

$$49 \quad \frac{3}{a+b}; \quad \frac{2}{a^2+ab} \qquad \left[\frac{3a}{a(a+b)}; \quad \frac{2}{a(a+b)} \right]$$

$$50 \quad \frac{2x}{x-y}; \quad \frac{4y}{x+y}; \quad \frac{1}{x^2-y^2} \quad \left[\frac{2x^2+2xy}{(x-y)(x+y)}; \quad \frac{4xy-4y^2}{(x-y)(x+y)}; \quad \frac{1}{(x-y)(x+y)} \right]$$

$$51 \quad \frac{2-x}{x^2+2xy+y^2}; \quad \frac{3+y}{x^2-y^2} \qquad \left[\frac{2x-2y-x^2+xy}{(x+y)^2(x-y)^2}; \quad \frac{3x+3y+xy+y^2}{(x+y)^2(x-y)} \right]$$

$$60 \quad \frac{3a}{3a+b} + \frac{b}{3a-b} + \frac{1-9a^2}{9a^2-b^2}$$

$$\left[\frac{1+b^2}{9a^2-b^2} \right]$$

$$61 \quad \frac{a-b}{a^2} + \frac{a}{a^2+ab} + \frac{b-a}{b^2+ab}$$

$$\left[\frac{3a^2b - b^3 - a^3}{a^2b(a+b)} \right]$$

$$62 \quad \frac{x}{2x+2y} - \frac{2y}{3x-3y} - \frac{2}{3}$$

$$\left[-\frac{x^2+7xy}{6(x^2-y^2)} \right]$$

$$63 \quad \frac{1}{x^2-y^2} + \frac{1}{x^2+2xy+y^2} - \frac{2}{x^2-2xy+y^2}$$

$$\left[\frac{-2y^2-6xy}{(x^2-y^2)^2} \right]$$

$$64 \quad a - \frac{3a}{a^3-1} - \frac{a^3-a^2}{a^2+a+1}$$

$$\left[\frac{2a^3 - a^2 - 4a}{a^3-1} \right]$$

79

$$\frac{a^2 - 4a + 4}{a^3 - 6a^2 + 12a - 8} + \frac{a}{4 - a^2}$$

$$\left[\frac{2}{(a-2)(a+2)} \right]$$

80

$$\frac{2x^2}{x^3 - 8} - \frac{x^2 + 2}{x^2 + 2x + 4} + \frac{1}{2 - x}$$

$$\left[\frac{-2x}{x^3 - 8} \right]$$

81

$$\frac{1}{2a + b} - \frac{1}{2a - b} - \frac{2b}{b^2 - 4a^2}$$

[0]

$$96 \quad \frac{3x}{4x-6y} \cdot \frac{4x^2-12xy+9y^2}{2x+3y} \cdot \left(-\frac{2}{x}\right) \quad \left[-\frac{6x-9y}{2x+3y}\right]$$

$$97 \quad \frac{a-1}{a} \cdot \left(-\frac{a^2+a+1}{2-a}\right) \cdot \frac{a-2}{a^3-1} \quad \left[\frac{1}{a}\right]$$

$$98 \quad \frac{2x-2}{x^2-6x+5} \cdot \frac{(x-5)^2}{4x} \cdot \left(-\frac{2x^2y}{5-x}\right) \quad [xy]$$

$$99 \quad \frac{a^6-a^5}{b^5-b^4} \cdot \frac{b^3-b^2}{a^4-a^3} \cdot (-1) \quad \left[-\frac{a^2}{b^2}\right]$$

$$113 \quad \left(\frac{4a^2 - 9}{a^4 - a} : \frac{4a^2 + 12a + 9}{1 - a^2} \right) : \frac{2a^2 - a - 3}{a + a^2 + a^3} \quad \left[-\frac{1}{2a + 3} \right]$$

$$114 \quad \left[\left(\frac{8 - a^3}{6ab} : \frac{2a - 4}{4 + 2a + a^2} \right) : \left(-\frac{3a^3 b^2}{2} \right) \right] : \frac{(a^2 + 2a + 4)^2}{18a^4} \quad \left[\frac{1}{b^3} \right]$$

$$129 \quad \left(\frac{4x^2y^3}{5z} \right)^3; \quad \left(-\frac{2x^6y}{z^2} \right)^3$$

$$\left[\frac{64x^6y^9}{125z^3}; -\frac{8x^{18}y^3}{z^6} \right]$$

$$130 \quad \left(-\frac{2a}{3b^2} \right)^4; \quad \left(\frac{bc^2}{5a^3} \right)^4$$

$$\left[\frac{16a^4}{81b^8}; \frac{b^4c^8}{625a^{12}} \right]$$

$$146 \quad \left(\frac{6x}{9x^2 - 1} - \frac{1}{3x + 1} - \frac{1}{3x - 1} \right) \cdot \left(\frac{2}{x + 1} - 3 \right)$$

$$\bullet 147 \quad \left(\frac{3x + 1}{3x - 1} - \frac{3x - 1}{3x + 1} \right) : \frac{4x^2}{1 - 3x}$$

$$148 \quad \left[(2 - x)^2 \cdot \left(\frac{1}{x^2 - 4} + \frac{1}{x + 2} \right) \right] : \left(\frac{x^2 - 2x + 1}{x - 1} \right)$$

$$149 \quad \left(\frac{2x^2}{x^3 - 8} - \frac{x + 2}{x^2 + 2x + 4} + \frac{1}{2 - x} \right) \cdot \frac{8 - x^3}{4}$$

$$164 \quad \left(\frac{5a+5}{a^2+3a+2} - 1 \right) \cdot \left(\frac{1}{2} + \frac{3a+6}{a^2-a-6} \right) \cdot (a+2) \quad \left[-\frac{a+3}{2} \right]$$

$$165 \quad \left(\frac{1}{y} + \frac{x}{xy-y^2} - \frac{y^3-x^3}{xy^3-x^3y} + \frac{y}{x^2+xy} \right) \cdot \frac{xy-y^2}{x} - 1 \quad [0]$$

$$166 \quad \left(\frac{5x-13}{2x^2-2} + \frac{6x-21}{2x+2} - \frac{3x-5}{x-1} \right) : \frac{3}{x^2+2x+1} + x \quad [-2x-3]$$